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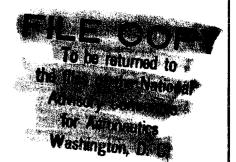
NATIONAL ADVISORY COMMITTEE FOR AERONAUTICS

TECHNICAL NOTE

No. 1196

INVESTIGATIONS OF EFFECTS OF SURFACE TEMPERATURE AND SINGLE ROUGHNESS ELEMENTS ON BOUNDARY-LAYER TRANSITION

By Hans W. Liepmann and Gertrude H. Fila California Institute of Technology





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SUMMARY

The laminar boundary layer and the position of the transition point were investigated on a heated flat plate. It was found that the Reynolds number of transition decreases as the temperature of the plate is increased. It is shown from simple qualitative analytical considerations that the effect of variable viscosity in the boundary layer due to the temperature difference produces a velocity profile with an inflection point if the wall temperature is higher than the free-stream temperature. This profile is confirmed by measurements. Furthermore, it is confirmed that even with large deviation from the Blasius condition, the velocity and temperature profiles are very nearly identical, as predictable theoretically for a Prandtl number σ of the order of 1.0 (for air, $\sigma = 0.76$). The instability of inflection-point profiles is discussed.

Studies of the flow in the wake of large, two-dimensional roughness elements are presented. It is shown that a boundary layer can separate and reattach itself to the wall without having transition take place.

INTRODUCTION

The problem of boundary-layer transition has been for several years the subject of research projects sponsored by the National Advisory Committee for Aeronautics. One part of the problem, the question of the stability of laminar flow, can be considered solved. (The problem of laminar instability should not be confused with the problem of predicting transition. For further details, see reference 1.) The experiments carried out at the National Bureau of Standards (reference 2) and at the California Institute of Technology (reference 3) agree very well with the results of Lin in a very complete theoretical analysis of laminar instability (reference 4), and there is no doubt that the laminar boundary layer first becomes unstable with respect to small perturbations at a certain critical Reynolds number R₁.

In the course of the experimental investigations, the effects of external turbulence, curvature, and pressure gradients on boundary-layer transition have been investigated. The present report treats principally investigations of two other factors, the effects of elevated surface temperature and of roughness elements upon the position of the transition point. The investigation of effects of this kind is prompted partially by practical considerations. The effect of roughness elements on transition is a question of obvious importance in connection with laminar-flow airfoils, and the effect of an increased surface temperature on the position of the transition point is of importance in connection with the use of thermal de-icing equipment on low-drag airfoils.

In addition to these practical considerations, both problems are of interest for an understanding of the general mechanism of transition. From the investigation of laminar instability (references 2 to 4), it is clear that certain disturbances will increase in any laminar boundary layer if the Reynolds number exceeds a critical value R_1 . The Reynolds number, R_2 , at which transition actually begins can be defined in a way which makes it possible to link R_2 to R_1 (reference 1). A rough estimate shows that, as is known from experimental evidence, R_2 can be quite large compared with R_1 . The difference between R_2 and R_1 depends upon the magnitude of the initial disturbances, for example, the external turbulence level, and upon the amount of amplification in the instability zone for this particular disturbance. For a given Reynolds number, the emount of amplification depends upon the shape of the mean-velocity profile.

Small roughness elements introduce disturbances into the laminar layer and thus precipitate transition. For example, regularly spaced small roughness elements can be used to introduce regular oscillations in the laminar boundary layer (reference 3). If the height of the elements is small compared with the boundary-layer thickness, there is no change in the mean-velocity profile and, therefore, no change in the amplification zone. Most earlier work on the influence of roughness on transition was concerned with investigations of uniformly distributed small roughness elements. (See, e.g., reference 5.) The measurements presented in the present report, however, are concerned with single, large, two-dimensional elements. The flow in the wake of a single roughness element is studied.

It should be noted that the flow in the wake of a single large roughness element in the boundary layer bears some similarity to the flow which exists on the upper surface near the leading edge of an airfoil at an angle of attack. The boundary-layer flow from the stagnation point around the nose of the airfoil is essentially similar to flow along a surface with a large roughness element (fig. 1). In fact, it is this effect — namely, the separation of a boundary layer from the wall and possible subsequent reattachment to the wall — which was of primary interest in the roughness study.

It is a well-known fact (e.g., reference 3) that a "free" laminar boundary layer becomes turbulent at a much lower Reynolds number than a normal "wall" boundary layer. Another important question, therefore, is whether the (laminar) separated layer becomes turbulent before reattachment to the wall or whether it is possible for the layer to remain laminar through the period of reattachment. This investigation was prompted by some previous interesting results on similar roughness elements (reference 3).

The surface temperature affects the position of the transition point in two distinctly different ways. One is essentially an effect of gravitational forces and due to the density differences in the boundary layer; the other effect is due to the dependence of the viscosity of the fluid upon its temperature, resulting in a change in the mean-velocity profile. The first effect has been discussed by Prandtl (reference 6) and Schlichting (reference 7) and was experimentally investigated by Reichardt (reference 8). This effect is due to the fact that for a stable configuration in a gravity field the density gradient should be directed downward (i.e., the denser fluid should be below). Thus air flow above a horizontal heated plate is destabilized, since the layers close to the plate have a higher temperature and a lower density. (A hot stream past a cold plate in the same configuration is stabilized.) The second effect was noted by Frick and McCullough (reference 9), who investigated the effects of internal heating, for the purpose of preventing formation of ice, on the characteristics of low-drag airfoils. The viscosity of a gas increases with increasing temperature. In laminar flow, as is shown later from the equation of motion, an increase in the wall temperature causes a negative viscosity gradient outward from the heated surface, which causes the appearance of inflection points in the boundary-layer profiles. The instability of inflection-point profiles is known (reference 4) to be larger than that of profiles with negative curvature throughout, and transition is thus hastened. This transition is the effect investigated in the present set of measurements.

This investigation, conducted at the California Institute of Technology, was sponsored by, and conducted with financial assistance from, the National Advisory Committee for Aeronautics. Dr. C. B. Millikan supervised the research. The authors wish to acknowledge the contribution of Mr. P. O. Johnson, who carried out the measurements on the roughness problem and designed the heated-plate unit. Discussions with Messrs. J. Laufer and S. Corrsin were very helpful.

SYMBOLS

X	distance along surface of plate from leading edge
у	distance perpendicular from surface of plate
U, V	local mean velocity in x- and y-directions, respectively
Uo	mean velocity of the free stream in the x-direction
u	x-component of velocity fluctuations
$\frac{\mathbf{u}}{\mathbf{U}} = \sqrt{\frac{\mathbf{u}^2}{\mathbf{U}^2}}$	root mean square of the u-velocity fluctuation level
ρ	density
μ	absolute viscosity
$q = \frac{1}{2} \rho U_0^0$	dynamic pressure of the free stream
p	static pressure
$v = \frac{\mu}{\rho}$	kinematic viscosity
$\eta = \sqrt{\frac{U}{px}} y$	Blasius' nondimensional parameter
t	time
$R = \frac{U_0 x}{v}$	Reynolds number using the parameter x
R_1	Reynolds number corresponding to lower limit of stability
$R_{\mathbf{Z}}$	Reynolds number corresponding to beginning of transition
x ₂	distance along surface of plate to beginning of transition
T	temperature, degrees centigrade
θ	temperature difference between wire and air, degrees centigrade
$\theta_{\rm u} = T_{\rm u} - T_{\rm f}$	temperature difference between a point in the boundary layer and the free stream, degrees centigrade

$\theta_{\mathbf{W}} = \mathbf{T}_{\mathbf{W}} - \mathbf{T}_{\mathbf{f}}$	temperature difference between wall and free stream, degrees centigrade							
$\sigma = \frac{v}{k}$	Prandtl number							
€	height of roughness element, inches							
đ	diameter of two-dimensional roughness element, inches							
H	rate of heat loss of hot wire to air							
А, В	hot-wire constants							
α	temperature coefficient of resistance of wire							
r	resistance of wire when heated to temperature T							
r_0	resistance of wire at temperature of OC C							
rf	resistance of unheated wire at temperature Tf in free stream							
r_{u}	resistance of unheated wire at temperature $T_{\rm u}$ at any point in the heated boundary layer							
r_{W}	resistance of unheated wire at temperature $\ensuremath{T_W}$ at the heated wall							
Subscripts								
W	wall							
f	free stream							
u	point in the heated boundary layer							

APPARATUS AND METHODS

Wind Tunnel and Plate Installation

The wind tunnel used for this investigation was constructed at the California Institute of Technology in 1938. It is of the Eiffel type with a 16-to-1 contraction ratio. The working section is 20 inches square and 12 feet long, and is provided with adjustable side walls to facilitate obtaining a constant velocity along its entire length. The power unit is a 5-horsepower direct-current motor driving a two-blade wooden fan 30 inches in diameter. A sketch of the tunnel is shown in figure 2(a).

A polished aluminum plate 1/4 inch thick and 19 inches wide was used for this work. The plate was 6 feet long and the leading edge was beveled to a sharp edge.

The plate was mounted vertically in the center of the wind tunnel on built-up grooves as shown in figure 2(b). The upper surface of the tunnel is removable in panels; thus adjustment of the upper edge of the plate to obtain a vertical plate was facilitated. The observation panel is 1/4-inch plate glass located on the upper tunnel surface, and is interchangeable with any of the removable panels. The roughness elements used in this investigation were wooden half-circular cylinders mounted on the plate as shown in figure 2(c).

The heating elements for the heated-plate experiments were mounted on the back of the plate, placed between two thin sheets of asbestos, and further insulated with cork backing. This resulted in a test plate of l_2^1 -inch thickness and thus necessitated adjustment of other physical factors in the tunnel to simulate flat-plate flow. The method used to accomplish this is discussed later in the report. The plate was heated from the leading edge to x = 75 centimeters. Figure 3 shows the test plate mounted in the test section of the wind tunnel.

Description of Hot-Wire Equipment

The hot-wire technique has been used extensively at the California Institute of Technology, and its use has been continued in these investigations. All measurements of velocity fluctuations were made with the hot-wire apparatus, and most of the velocity profiles were obtained by this method. (A hypodermic-needle total-head tube was used to verify the hot-wire results obtained when investigating the velocity distribution of the boundary layer on a heated plate.) The determination of the transition point was made by means of a hot-wire anemometer and an oscilloscope.

The hot wire.— The hot wire used in these experiments was constructed of copper lead—in wires, ceramic tubing, fine sewing needles, and the platinum wires 0.0005 and 0.00024 inch in diameter for mean—speed and velocity—fluctuation measurements, respectively. Two copper wires were thrust through small holes in a 4—inch length of ceramic tubing for mean—speed measurements and measurements of the fluctuations parallel to the mean flow. These wires were cemented into the tubing at both ends, and needles were soldered to them. The platinum hot wire was then soft—soldered across the tips of the sewing needles. (The silver cover of the 0.00024—inch Wollaston wire was removed by immersion in nitric acid before the wire was soldered to the needles.)

The 0.0005-inch wires used for measuring mean speed were generally about 3 millimeters long. Velocity fluctuations parallel to the mean flow u' were measured with a single wire about 2 millimeters long.

Mean-speed measurement and equipment.— For measuring mean speed, the constant-resistance method was employed. A description of this method may be found in reference 10. A slight variation of this method was necessary, however, when measuring the profile of the heated-plate boundary layer; namely, the wire was maintained at a constant temperature rise above the local air stream. The measuring instruments consisted mainly of a Wheat-stone bridge for obtaining the resistance of the wire, and a potenti-ometer for measuring the current through the wire or the voltage drop across the wire. This mean-speed apparatus with the necessary switching devices, together with the amplifier, was built into one large steel cabinet to minimize electrical pickup.

The amplifier.—A four-stage alternating-current amplifier as described in earlier reports (references 1 and 3) was used to amplify the voltage fluctuations across the hot wires. The gain of the amplifier was constant within 2 percent between about 5 and 8000 cycles per second. A standard inductance-resistance compensation circuit was provided and used in all turbulence measurements.

Traversing mechanism.— A complete investigation of the boundary layer and of transition requires a continuous traverse with the measuring instrument along the plate in the direction of air flow and normal to the plate (in y-direction). The hot-wire carriage as shown in figure 4 is constructed of three aluminum legs and a gear train with micrometer attachment for transporting the hot wire in the y-direction. The carriage is moved along the tunnel on a track by a 120-volt alternating-current motor, and the movement in the y-direction is controlled by a 6-volt direct-current motor. Switches outside the tunnel enable the operator to control the position of the hot wire in both directions, and substitution of a glass plate for the usual wooden top panel permits reading of the micrometer giving y-position.

Turbulence Level in the Tunnel

The turbulence level in the working section is reduced by a honeycomb and a screen in the forward part of the wind tunnel. The honeycomb is at the intake of the tunnel and serves mainly to smooth the very irregular flow entering the tunnel. It is of spot-welded construction, having 1/2-inch cells with a depth of $4\frac{1}{2}$ inches. The screen is located 55 inches behind the honeycomb and is a seamless precision screen with 18 mesh per inch and a wire diameter of 0.018 inch. The free-stream turbulence level in this tunnel is $\frac{u^2}{U} = 0.0005$; $\frac{v^2}{U} = \frac{w^2}{U} = 0.0008$.

Artificial turbulence was introduced for one particular phase of the investigation on the heated plate. Strips of notebook paper 1 by 6 inches were strung 6 inches apart on wires just upstream of the screen. The turbulence level in the test section was then determined to be 0.17 percent. Figure 5 shows the method of mounting the paper strips; the honeycomb was rolled away for the picture.

Heating the Plate

The plate was heated by means of nichrome resistance wires mounted on the back of the flat plate. The elements were more closely spaced near the leading edge since it was evident that for a given wall temperature the rate of heat transfer to the boundary layer would be larger near the leading edge, where the gradients are larger. The temperature of the plate was controlled by grouping the heating elements into four separate circuits and inserting an external variable resistance in each circuit. Thus the temperature gradient along the plate was made nearly zero (see fig. 6) by varying the resistance when the plate temperature had reached equilibrium with the air flowing.

The temperature along the plate was determined by a copper-constantan thermocouple mounted in the traversing mechanism. Readings were taken at intervals of 5 centimeters along the plate. Voltages were read with a Leeds and Northrup potentiometer, and the corresponding temperature obtained from a standard calibration chart. The cold junction was maintained at room temperature. The accuracy of the apparatus was determined to be in the neighborhood of $\pm 1/2^{\circ}$ C. A permanent thermocouple was installed at x = 45 centimeters for continuous observation of the plate temperature. All heated-plate mean-speed measurements were taken with a plate temperature of 115° C $\pm 5^{\circ}$.

Figure 6 presents the temperature distribution along the heated plate maintained in equilibrium with a free-stream velocity of 8.19 meters per second. Two methods were used to bring the plate to the desired temperature. For the mean-speed and mean-temperature measurements, for which it was desired to obtain equilibrium as rapidly as possible, the current was applied to the heating circuits while the air in the tunnel was still. After approximately 25 minutes, when the plate temperature had reached 120°C, the wind tunnel was turned on and the temperature of the plate was allowed to reach equilibrium with a free-stream velocity of 8.19 meters per second. In the investigation of the effect of heating the flat plate on the location of the transition, the tunnel was operated at the desired free-stream velocity and the variation in the position of early turbulent bursts was noted as the plate heated up to its equilibrium temperature. The temperature as a function of time for heating is shown in figure 7.

Measurement of Pressure Distribution

A small total-head tube made from a hypodermic needle and a similar small static tube, mounted together, were used in measuring the pressure distribution along the plate. The total-head tube was a number-20-gage hypodermic needle flattened to 0.0165 inch in the y-direction, and the static tube was a 1/16-inch-diameter brass tube of standard design. They were mounted in the traversing mechanism just cutside the boundary layer. The pressure along the plate was measured with an alcohol manometer at this constant distance. Figure 8 shows the pressure distribution for both roughness and surface-temperature investigations.

For the roughness-element tests it was necessary to adjust the side walls only slightly to obtain $\frac{dp}{dx} = 0$, and thus to obtain a velocity

profile of the Blasius type. The addition of the equipment for heating the plate, however, resulted in a plate thickness of $1\frac{1}{2}$ inches. This finite thickness necessitated tunnel adjustments to preserve Blasius' flat-plate flow — that is, to obtain a negligible pressure gradient and to put the stagnation point on the "working" side of the plate. A transverse screen near the trailing edge of the plate, which increased the resistance to air flow on the working side of the plate, served to solve the problem of pressure gradient. The plate supports were adjusted to give a slightly favorable angle of attack to the plate (approx. $1/2^{\circ}$). Then, satisfactory Blasius flat-plate flow was obtained as shown in the velocity distribution of figure 9.

Determination of Transition Point

The method used for determination of the beginning of transition was that described in reference 3. This method consists in visual observation of velocity fluctuations measured by a hot-wire instrument and observed on the screen of a cathode-ray oscilloscope. The first appearance of turbulent bursts — that is, occasional sudden changes from a laminar profile to a turbulent profile — is taken as the transition criterion.

Computation of Heated-Plate Velocity

and Temperature Profile

For a hot-wire anemometer the relationship between heat loss and airspeed is given by the well-known King equation,

$$H = (A + B \sqrt{U})\theta$$

where θ is the temperature difference between wire and fluid, and A and B are constants for a given fluid.

In general,

$$\theta = \frac{\mathbf{r} - \mathbf{r}_{\mathbf{u}}}{\mathbf{r}_{\mathbf{u}}}$$

and for steady state, H = i2r. Then there can be written,

$$\frac{i^2r}{r-r_u} = A' + B' \sqrt{U}$$

where
$$A^{\dagger} = \frac{A}{r_0 \alpha}$$
 and $B^{\dagger} = \frac{B}{r_0 \alpha}$.

Both A and B are functions of the absolute temperature of the air, because of appreciable variations in the thermal conductivity and density (reference 11). The mean-velocity calibration of the hot wire was carried out at room temperature and then, in computing velocity profiles, the values were corrected to the temperature of the air at each measuring point.

The temperature distribution was measured by using the hot wire as a resistance thermometer; that is, the "cold" resistances of the hot wire \mathbf{r}_{u} , measured with negligible heating current, gives a direct measure of air temperature.

Since

$$r_{\rm u} = r_{\rm f}(1 + \alpha \theta_{\rm u})$$

and

$$r_{w} = r_{f} (1 + \alpha \theta_{w})$$

then

$$\frac{\theta_{u}}{\theta_{w}} = \frac{r_{u} - r_{f}}{r_{w} - r_{f}}$$

In order to get a direct comparison between the velocity and temperature distributions, the following equation is plotted:

$$1 - \frac{\theta_{\mathbf{u}}}{\theta_{\mathbf{w}}} = \frac{\mathbf{r}_{\mathbf{w}} - \mathbf{r}_{\mathbf{u}}}{\mathbf{r}_{\mathbf{w}} - \mathbf{r}_{\mathbf{f}}}$$

MEASUREMENTS AND RESULTS

Effect of Surface Temperature

Mean-velocity distribution.— The mean-speed distribution in the boundary layer of the heated flat plate was measured using both the hotwire anemometer and the impact tube. During these measurements a peculiar difficulty was encountered: General analytical considerations, discussed in a further section of the report, show that the velocity profile near a heated flat plate should be an inflection-point profile. Also, this type of profile is indicated in the measurements of Frick and McCullough in reference 9. Indeed, the observed velocity profiles generally show this behavior, as is seen in figure 10. The temperature distribution exhibits a behavior very similar to that of the velocity distribution (fig. 11), as is to be expected since the Prandtl number σ for air is close to unity ($\sigma = 0.76$).

On some days, however, no consistent velocity profile could be obtained. In these cases both hot-wire and impact-tube measurements showed a large scatter, and no reasonable profile could be measured. Figure 12 shows a typical set of these measurements. Much time has been spent in efforts to evaluate this effect quantitatively, without much Qualitatively, the process appears to be as follows: The heated plate was mounted vertically in order to avoid complications in the investigation due to the Prandtl instability, that is, the instability (or stability) due to gravitational effects. The boundary layer of a heated plate mounted vertically is neutrally stable with respect to this Prandtl instability. Cravitational effects will be present, however, so that the heated layers of air close to the surface will have a tendency to rise. This effect probably introduces secondary flow into the boundary layer, especially in the case of a comparatively small tunnel like the one in which the present measurements were made. It is believed that this secondary flow causes the indefinite velocity profiles, such as that shown in figure 11. The reasons why these secondary currents occur only a part of the time are not understood. It may well depend upon accidental starting conditions similar to the case in the Pai measurements on rotating cylinders (reference 12). It is believed that the transition measurements taken at times when the meanvelocity distribution was found normal are not essentially influenced by secondary motion.

Transition point. The transition point was determined as a function of the surface temperature for two values of the free-stream turbulence

level, $\frac{u^{\dagger}}{U_{O}} = 0.05$ and 0.17 percent. The results are presented in fig-

ure 13, where the distance of the transition point from the leading edge of the plate is plotted as a function of the surface temperature. The effect is obviously quite pronounced; with increasing temperature the transition point moves closer to the leading edge of the plate. The same results are replotted in figures 14 and 15 in terms of Reynolds number of transition against surface temperature.

The kinematic viscosity varies with temperature and thus varies across the boundary layer. It is therefore possible to base the Reynolds number on at least two particular values of the kinematic viscosity: that at the wall $v_{\rm W}$ and the value in the free stream $v_{\rm f}$. The Reynolds number of the transition based on $v_{\rm f}$ and the Reynolds number based on $v_{\rm W}$ are presented as functions of the temperature in figures 14 and 15, respectively. The length used in forming the Reynolds number is in both cases the distance from the leading edge.

The value of R₂ for zero temperature difference between the stream and the plate is very small, considering the low free-stream turbulence level existing in this tunnel. This small value of R₂ is due to the transverse contamination effect described by Charters (reference 13): The largest possible length, measured from the leading edge, of a laminar boundary layer is limited by contamination from the top and the bottom. Since the measurements had to be carried out at a low velocity (8.19 m/sec) the maximum possible Reynolds number is comparatively small.

Effect of Roughness Elements

The mean-speed distribution in the wake of the half-cylindrical roughness elements of 1/8- and 1/16-inch height have been measured with the hot-wire anemometer. The roughness elements were mounted on the flat plate at a distance of 50 centimeters from the leading edge for the investigation of the effect in the laminar boundary layer, and at a distance of 140 centimeters from the leading edge for the investigation of the effect in the turbulent layer. Figures 16 and 17 present the results of these measurements in the case where the element is placed in the laminar layer. Three typical cases can be distinguished. At the lowest speed (fig. 16(a)) the flow, after passing over the roughness element, returned to the surface and continued in the laminar state for some distance downstream. When the velocity was increased, the flow returned to the surface still laminar, but transition occurred almost immediately after the layer reached the surface of the plate (fig. 16(b)). When the velocity was increased still further, the flow became turbulent in the free boundary layer in the wake of the obstacle (fig. 16(c)) and returned to the surface in the turbulent state. Figures 17(a) and 17(b) show similar effects behind the larger roughness element.

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The elements were then placed in the turbulent boundary layer at a distance of 140 centimeters from the leading edge and the mean-velocity profiles again were measured downstream of the element. Figure 18 shows a typical result of these measurements. The velocity distribution in this figure is plotted against the logarithm of the distance from the 'wall. It is seen that the velocity profile returns rapidly to a "normal" turbulent profile, which is represented, of course, by a straight line in the logarithmic plot.

These experiments are not to be considered as a quantitative investigation. They are intended to show the types of physical phenomena connected with boundary-layer flow past roughness elements. A more complete investigation requires a larger tunnel in which thicker boundary layers can be obtained without introducing secondary flow.

DISCUSSION

Mean-Velocity Profile near a Heated Wall

The laminar-boundary-layer equation in the absence of a pressure gradient for two-dimensional flow past a wall of negligible curvature is

if $\mu = \mu(y)$.

If the wall is approached, U and V approach zero, and thus

$$\left[\frac{\partial \lambda}{\partial u} \left(u \frac{\partial \lambda}{\partial \Omega} \right) \right]^{\lambda = 0} = 0$$

Hence the curvature of the velocity profile at the wall becomes

$$\left(\frac{\partial^{\lambda}}{\partial_{s}\Omega}\right)^{\lambda=0} = -\frac{h^{\lambda=0}}{J} \left(\frac{\partial^{\lambda}}{\partial h}\right)^{\lambda=0} \left(\frac{\partial^{\lambda}}{\partial \Omega}\right)^{\lambda=0}$$

If the surface is heated, the temperature will drop with increasing y. For a gas, μ increases with temperature, and consequently

$$\frac{9}{9}\frac{\Lambda}{\Pi} < 0$$

¹March 1947: Mr. L. Lees has recently computed the complete temperature and velocity profiles. His results have not yet been published.

Since the velocity U increases with y,

$$\frac{\partial^{\Lambda}}{\partial \Omega} > 0$$

and thus

$$\left(\frac{9^{\lambda_S}}{9_{SD}}\right)^{\lambda=0} > 0$$

if the surface temperature $\mathbf{T}_{\mathbf{W}}$ is higher than the free-stream temperature $\mathbf{T}_{\mathbf{f}}$.

At the edge of the boundary layer, U approaches the constant free-stream velocity $U_{\rm C}$ asymptotically, and hence

$$\frac{9^{\Lambda_S}}{9_S \Lambda} < 0$$

at the edge of the layer. Consequently,

$$\frac{\partial \lambda_{S}}{\partial_{S}\Pi} = 0$$

at some point within the boundary layer.

The effect of surface temperature is similar to the effect of a pressure gradient. In the case of a pressure gradient, and zero temperature gradient, an analogous discussion gives

$$\left(\frac{\partial \lambda_{S}}{\partial_{S}\Omega}\right)^{\lambda=0} = \frac{\pi}{I} \frac{\partial x}{\partial b}$$

and thus

$$\left(\frac{\partial \lambda_{s}}{\partial_{s}n}\right)^{\lambda=0} > 0$$

if p increases with x, that is, in the case of an "adverse" pressure gradient. Both of these effects are evidently independent of p.

Instability of Inflection-Point Profiles

Tollmien (reference 14) obtained the theoretical result that inflection-point profiles are always unstable. Based on this result, inflectionpoint profiles have been considered as distinguished sharply from normal. profiles, that is, profiles with negative curvature throughout. Lin's analysis (reference 4) shows that such a sharp distinction cannot be drawn. Lin shows that a difference in the stability character of normal and inflection-point profiles becomes apparent only for very large Reynolds numbers. The range of wave lengths of unstable perturbations (see references 2 to 4) tends to zero if the Reynolds number approaches infinity for the normal profile, but remains finite as the Reynolds number approaches infinity for the inflection-point profiles. This result is in fact not contradictory to Tollmien, since Tollmien's considerations are restricted to a nonviscous fluid, which simply means the Reynolds number approaches infinity. Lin's considerations do show, however, that the instability of a profile - that is, the critical Reynolds number, the extent of the range of unstable wave lengths, and so forth - depends on the magnitudes of the slope and of the curvature of the velocity profile near the wall. In fact, it shows that inflection-point profiles generally do have a lower critical Reynolds number and a larger zone of unstable wave lengths than normal profiles. Consequently, transition in the boundary layer of a gas flow is hastened by an increased surface temperature because inflection-point profiles develop. It is interesting to note that surface temperature should have the opposite effect in a liquid; there the viscosity decreases with increasing temperature, and consequently in the velocity profile of a liquid on a heated surface

$$\left(\frac{9^{\lambda_5}}{9_{5^{\Omega}}}\right)^{\lambda=0} < 0$$

Laminar Separation and Transition

It has been assumed in some earlier considerations of laminar boundary layers that transition sets in immediately at the point of separation. In fact, in attempts to compute and predict transition, it has often been assumed that it is sufficient to show that at some place in the laminar layer a separation profile, that is, a velocity profile which has a normal tangent at the wall, develops.

The results of the surveys in the wake of the obstacles show that the existence of a separation profile does not necessarily lead to transition. In figure 16, for example, the boundary layer is separated from the solid boundary for a considerable distance downstream from the roughness element and still remains laminar, even after reattachment.

A second problem of laminar separation and transition is the following: With the assumption that the boundary layer becomes turbulent in the detached condition (as, for example, in figs. 16(c) and 17(c)), determine the velocity profile that exists after the turbulent free layer has reattached to the wall. The measurements (figs. 16(c) and 17(b)) show that, in the investigated configuration, the velocity profile transforms very rapidly to a normal turbulent-boundary-layer profile, that is, the logarithmic type profile. The same rapid transformation to a logarithmic profile also occurs if the element is placed in the turbulent layer (fig. 18).

It should be very interesting to investigate whether a turbulent separated profile always changes to a logarthmic profile as rapidly as in these measurements of flow past a flat plate. For example, the influence of an adverse pressure gradient and of curvature of the solid boundary appears to be of interest in connection with the problem of laminar separation and subsequent reattachment of the boundary layer near the leading edge of airfoils. Problems of this kind are thought to be quite important in connection with the design of sharp-nose airfoils for high-speed flow.

CONCLUDING REMARKS

An increased temperature of the wall hastens boundary-layer transition. This result confirms earlier measurements of Frick and McCullough. In investigating the influence of surface temperature on transition, two effects must be distinguished: an effect due to gravitational forces and an effect due to the dependence of the viscosity of a gas on the temperature. The second effect is the one investigated here and also by Frick and McCullough. The dependence of the viscosity on the temperature, if the fluid is a gas, leads to velocity profiles with positive curvature at the wall and therefore greater instability for a heated wall than an unheated one.

Furthermore, it is confirmed that, even with large deviation from the Blasius condition, the velocity and temperature profiles are very nearly identical, as predictable theoretically for a Prandtl number σ of the order of 1.0 (for air, $\sigma = 0.76$).

Studies of air flow in the wake of large two-dimensional roughness elements show that a laminar boundary layer can separate from the wall and reattach itself without transition taking place. If transition takes place in the detached layer, the velocity profile in the reattached boundary layer will approach the normal turbulent-boundary-layer profile very rapidly.

California Institute of Technology,
Pasadena, Calif., August 28, 1946.

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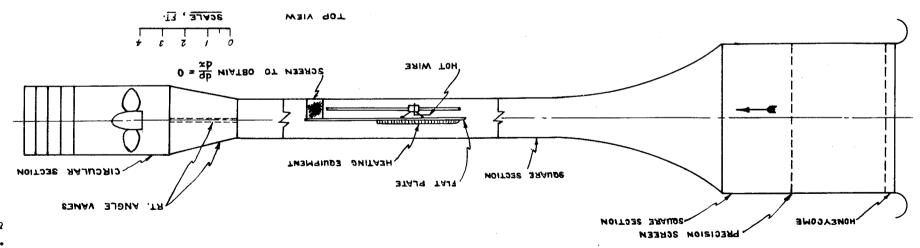
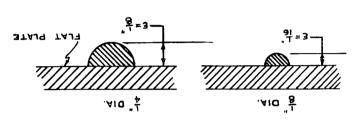


FIGURE 2 A. - SCHEMATIC DIAGRAM OF THE WIND TUNNEL.



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FIGURE 2 .. - MOUNTING OF ROUGHNESS ELEMENTS.

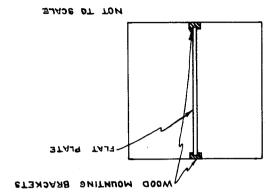
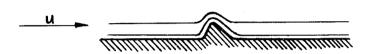


FIGURE 2. - MOUNTING OF FLAT PLATE,



BOUNDARY-LAYER FLOW FROM THE STAGNATION POINT AROUND THE NOSE OF AN AIRFOIL AT A SMALL ANGLE OF ATTACK.



BOUNDARY-LAYER FLOW ALONG A SURFACE WITH A LARGE, SINGLE ROUGHNESS ELEMENT.

FIGURE 1.- SIMILARITY OF FLOW NEAR A SHARP LEADING EDGE AND OVER A ROUGHNESS ELEMENT ON A FLAT PLATE.

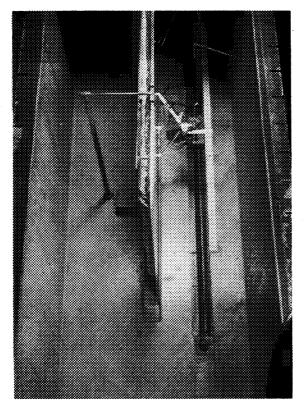


Figure 3.- Test plate mounted in the working section of the wind tunnel with the top panels removed. Photograph taken from above and upstream.

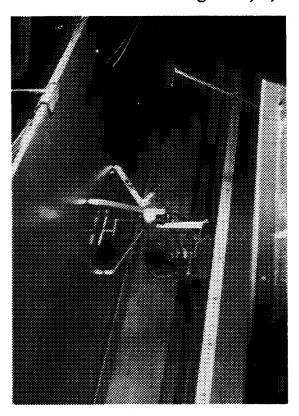


Figure 4.- Traversing mechanism.

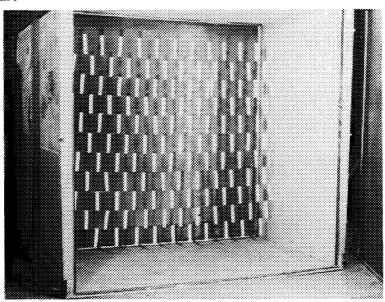


Figure 5.- Method of mounting paper strips to create artificial turbulence in the tunnel.

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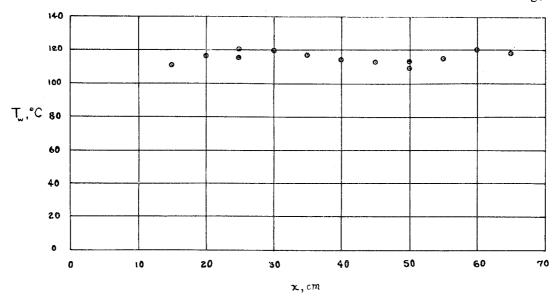


FIGURE 6. - TEMPERATURE DISTRIBUTION ALONG THE HEATED PLATE.

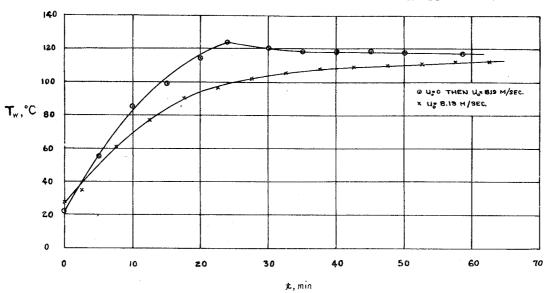


FIGURE 7. - TWO METHODS OF HEATING THE FLAT PLATE.

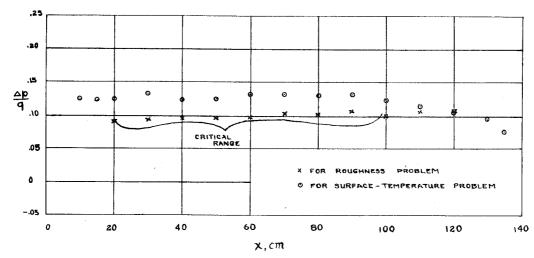


FIGURE 8. - PRESSURE DISTRIBUTION ALONG THE TEST PLATE.

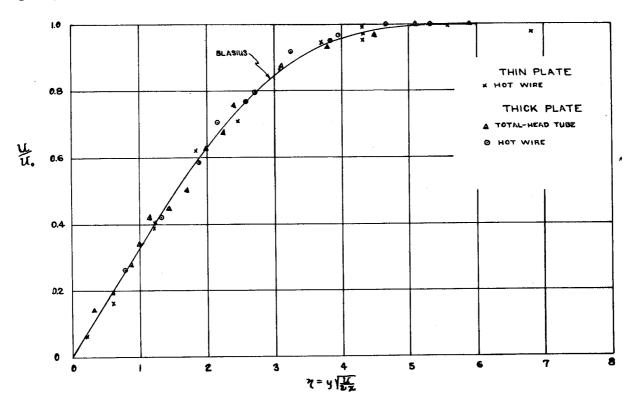


FIGURE 9. - VELOCITY DISTRIBUTION IN THE BOUNDARY LAYER OF THE UNHEATED FLAT PLATE.

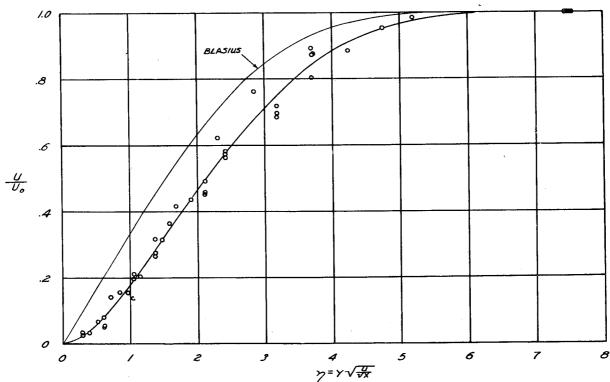


FIGURE 10. ~ VELOCITY DISTRIBUTION IN THE BOUNDARY LAYER OF THE HEATED PLATE.

REGULAR PROFILE CONFIRMING ANALYTICAL CONSIDERATIONS.

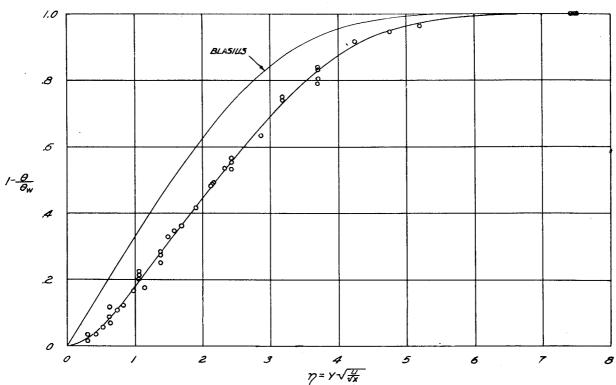


FIGURE 11. TEMPERATURE DISTRIBUTION IN THE BOUNDARY LAYER OF THE HEATED PLATE,
REGULAR PROFILE CONFIRMING ANALYTICAL CONSIDERATIONS.

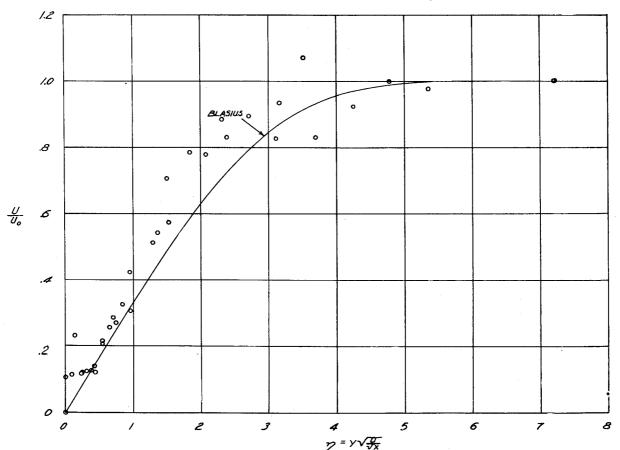


FIGURE 12a - VELOCITY DISTRIBUTION IN THE BOUNDARY LAYER OF THE HEATED PLATE.

UNPREDICTED PROFILE DUE PROBABLY TO SECONDARY FLOW.

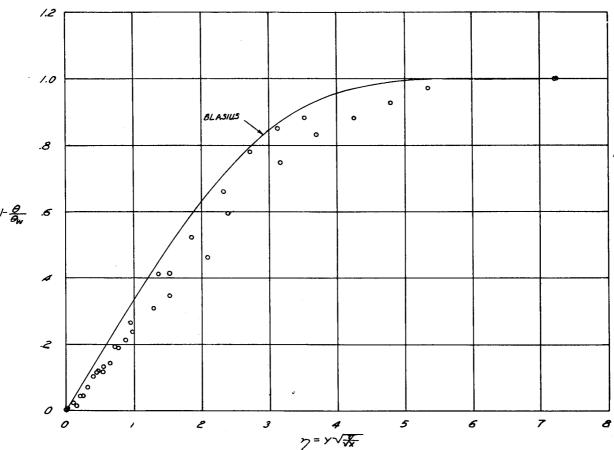


FIGURE 126.—TEMPERATURE DISTRIBUTION IN THE BOUNDARY LAYER OF THE HEATED PLATE.

UNPREDICTED PROFILE DUE PROBABLY TO SECONDARY FLOW,

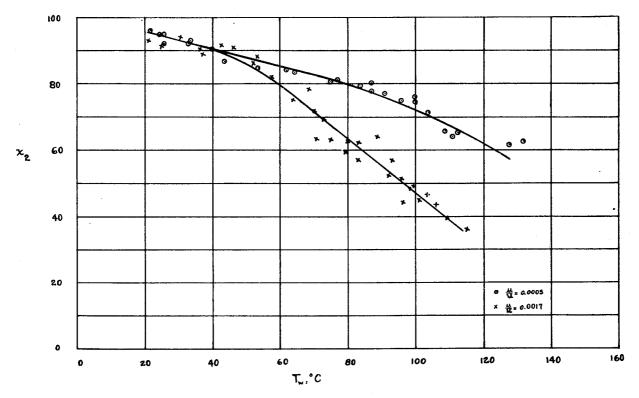


FIGURE 13. - EFFECT OF PLATE TEMPERATURE ON TRANSITION.

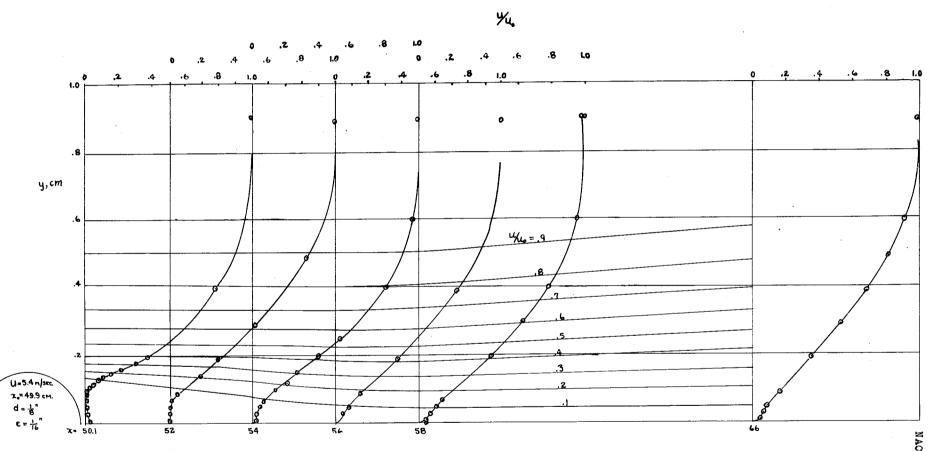


FIGURE 164 - VELOCITY PROFILES DOWNSTREAM FROM A SMALL ROUGHNESS ELEMENT.

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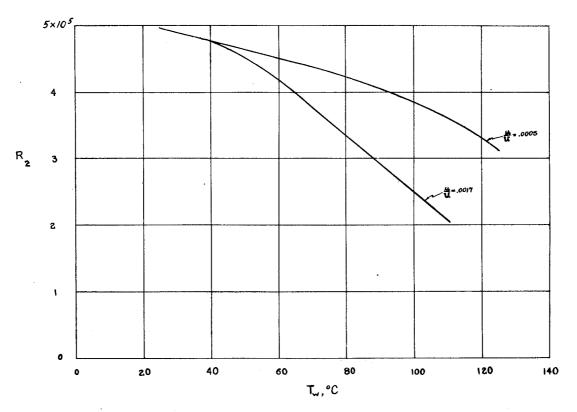


FIGURE 14. - EFFECT OF PLATE TEMPERATURE ON THE REYNOLDS NUMBER OF TRANSITION (PERE STREAM).

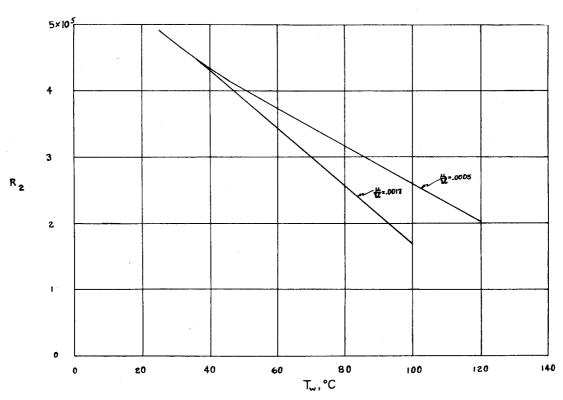
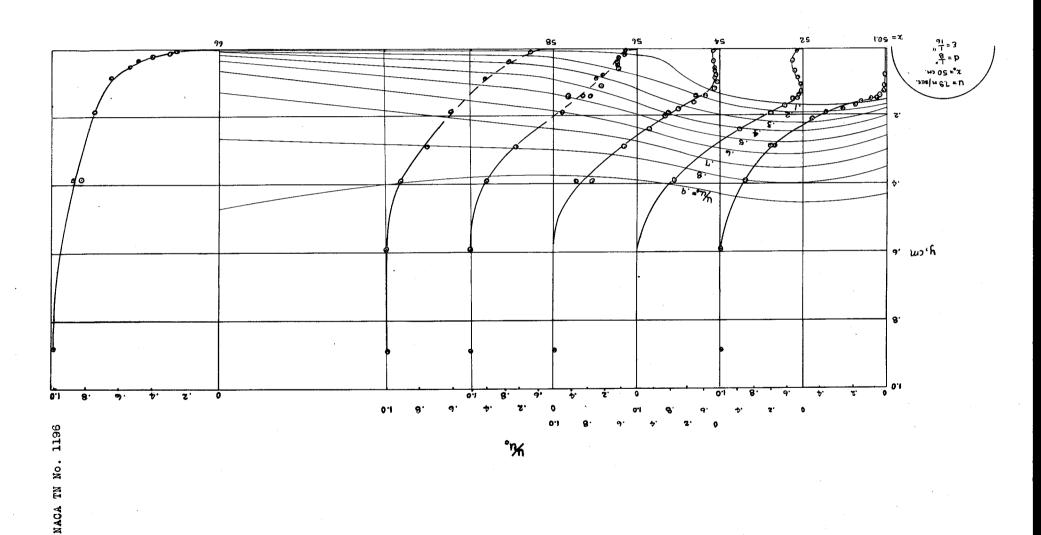


FIGURE 15. - EFFECT OF PLATE TEMPERATURE ON THE REYNOLDS NUMBER OF TRANSITION (V).



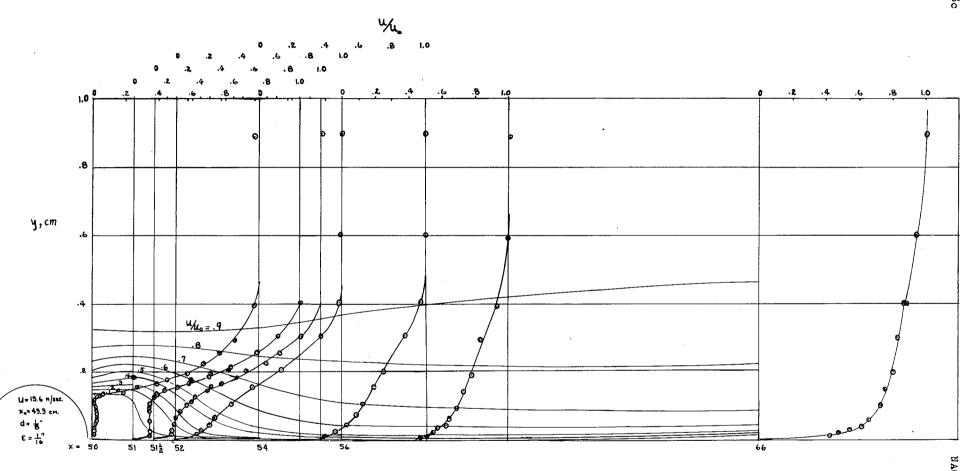
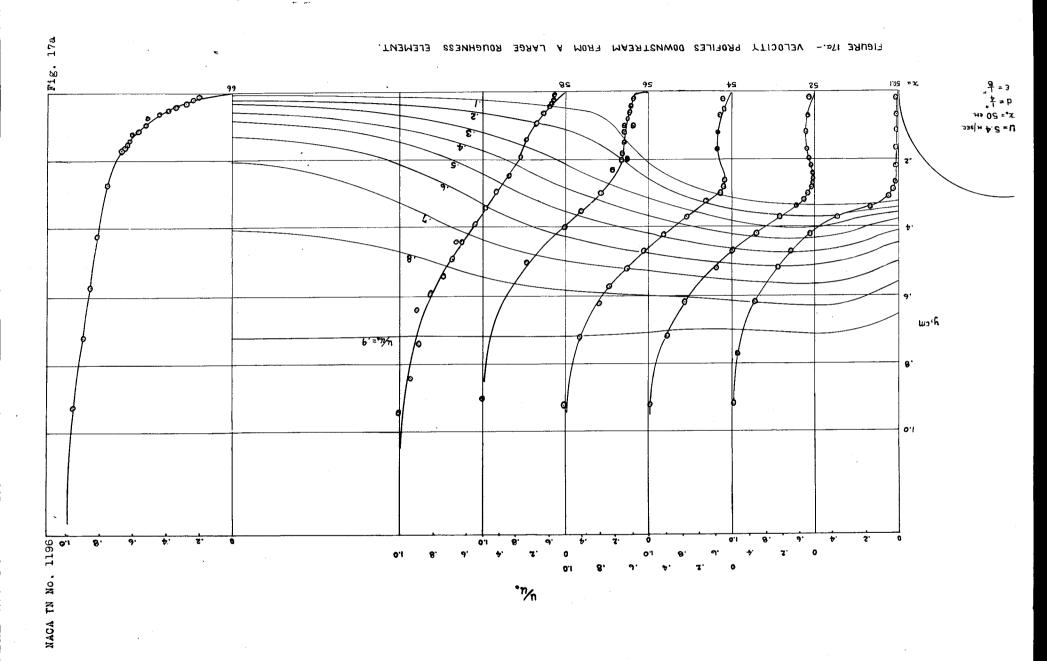


FIGURE 160. F VELOCITY PROFILES DOWNSTREAM FROM A SMALL ROUGHNESS ELEMENT.





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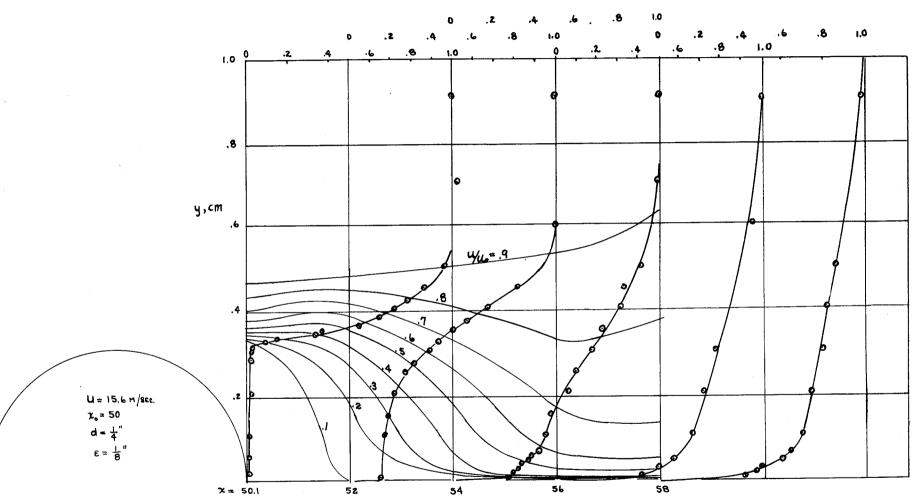


FIGURE 176 .- VELOCITY PROFILES DOWNSTREAM FROM A LARGE ROUGHNESS ELEMENT.

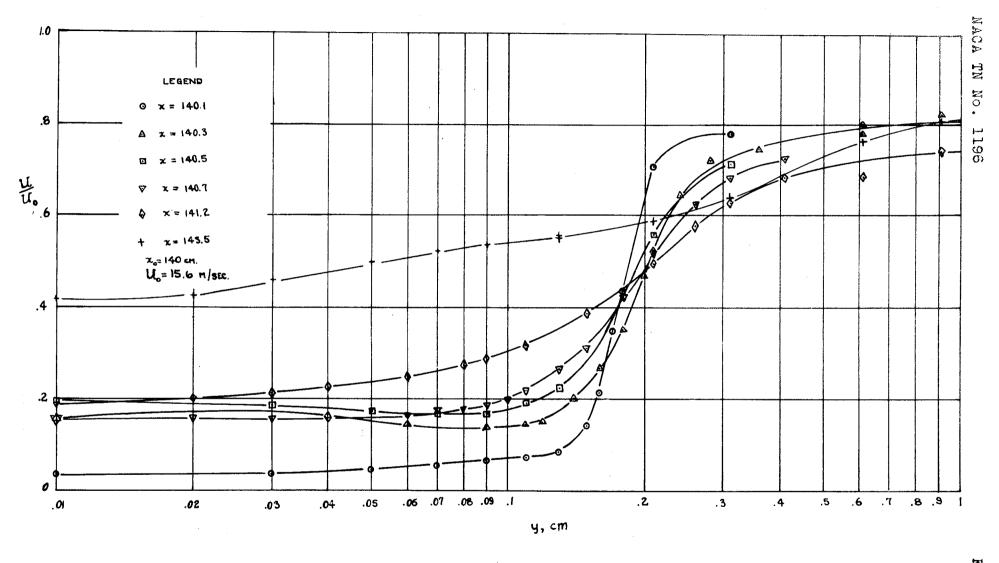


FIGURE 18. - LOGARITHMIC PLOT OF TURBULENT-VELOCITY PROFILES DOWNSTREAM FROM A ROUGHNESS ELEMENT.

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